

ARMY RESEARCH LABORATORY

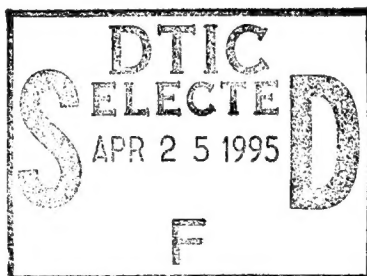


# Poisson's Ratio for Tetragonal Crystals

Arthur Ballato

ARL-TR-423

March 1995



19950421 090

UNCLASSIFIED

APPROVED FOR PUBLIC RELEASE; DISTRIBUTION IS UNLIMITED.

## **NOTICES**

### **Disclaimers**

The findings in this report are not to be construed as an official Department of the Army position, unless so designated by other authorized documents.

The citation of trade names and names of manufacturers in this report is not to be construed as official Government endorsement or approval of commercial products or services referenced herein.

# REPORT DOCUMENTATION PAGE

Form Approved  
OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.

1. AGENCY USE ONLY (Leave blank)		2. REPORT DATE March 1995	3. REPORT TYPE AND DATES COVERED Technical Report	
4. TITLE AND SUBTITLE POISSON'S RATIO FOR TETRAGONAL CRYSTALS			5. FUNDING NUMBERS	
6. AUTHOR(S) Arthur Ballato				
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) US Army Research Laboratory (ARL) Electronics and Power Sources Directorate (EPSD) ATTN: AMSRL-EP Fort Monmouth, NJ 07703-5601			8. PERFORMING ORGANIZATION REPORT NUMBER ARL-TR-423	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)			10. SPONSORING/MONITORING AGENCY REPORT NUMBER	
11. SUPPLEMENTARY NOTES				
12a. DISTRIBUTION/AVAILABILITY STATEMENT Approved for public release; distribution is unlimited.			12b. DISTRIBUTION CODE	
13. ABSTRACT (Maximum 200 words) General expressions for Poisson's ratio are derived for tetragonal crystals; simplified forms are given for cases involving symmetry directions.				
14. SUBJECT TERMS Isotropic media; tetragonal symmetry			15. NUMBER OF PAGES 13	
			16. PRICE CODE	
17. SECURITY CLASSIFICATION OF REPORT Unclassified	18. SECURITY CLASSIFICATION OF THIS PAGE Unclassified	19. SECURITY CLASSIFICATION OF ABSTRACT Unclassified	20. LIMITATION OF ABSTRACT UL	

## TABLE OF CONTENTS

Section	Page
Abstract	1
Introduction	1
Expressions Relating Tetragonal Stiffnesses and Compliances	2
Definition of Poisson's Ratio for Crystals	3
Relations for Rotated Tetragonal Compliances - General	3
Single-Axis Rotations	3
Transformation Matrix for General Rotations	5
Poisson's Ratios for Specific Orientations	5
Conclusions	6
Bibliography	7

Accession For	
NTIS	<input checked="" type="checkbox"/> CRA&I
DTIC	<input type="checkbox"/> TAL
Unannounced	<input type="checkbox"/>
Justification	
By	
Distribution /	
Availability Codes	
Dist	Avail and/or Special
A-1	

## POISSON'S RATIO FOR TETRAGONAL CRYSTALS

### Abstract

General expressions for Poisson's ratio are derived for tetragonal crystals; simplified forms are given for cases involving symmetry directions.

### Introduction

Poisson's ratio,  $\nu$ , is defined for isotropic media as the quotient of lateral contraction to longitudinal extension arising from application of a simple tensile stress; in most materials, this dimensionless number is positive. In crystals,  $\nu$  takes on different values, depending on the directions of stress and strain chosen. The ratio finds application in a variety of areas of applied elasticity and solid mechanics, for example, as indication of the mechanical coupling between various vibrational modes of motion.

The maximum value of  $\nu = +1/2$  is obtained in the incompressible medium limit, where volume is preserved; for ordinary materials, values of  $+1/4$  to  $+1/3$  are typical, but in crystals  $\nu$  may vanish, or take on negative values. Analytical formulas for Poisson's ratio are expressed in terms of elastic constants. For the case of crystals of general anisotropy, these expressions are quite unwieldy, but for tetragonal crystals the symmetry elements reduce the complexity considerably.

Crystals of tetragonal symmetry include a number of ferroelectrics as well as lithium tetraborate, a nonferroelectric with substantial piezoelectric coupling and temperature-compensated properties. These materials are potentially important for high technology applications such as cellular radio and microwave collision avoidance radar. Each of the seven tetragonal point groups is characterized by one of two elastic matrix schemes, so it is necessary to distinguish among the point groups. The distinction relates to symmetry: those groups that appear as holohedral under classical x-ray analysis (classes  $4\text{-}\bar{2}m$ ,  $422$ ,  $4mm$ , and  $4/m\text{-}2\text{-}2$ ) have an elastic matrix in which  $c_{16}$  and  $s_{16}$  constants do not appear; the remainder (classes  $4\text{-}\bar{2}$ ,  $4$ , and  $4/m$ ) retain the  $c_{16}$  and  $s_{16}$  entries. The presence of piezoelectricity is neglected.

## Expressions Relating Tetragonal Stiffnesses and Compliances

Relations for Poisson's ratio are most simply expressed in terms of the elastic compliances  $[s_{\lambda\mu}]$ . It is often the case, however, that the most accurate determinations of the elastic constants (resonator and transit-time methods) yield values for the stiffnesses  $[c_{\lambda\mu}]$  directly; the conversion relations are given below. For the tetragonal system, the elastic stiffness and compliance matrices have identical form. Referred to the  $x_k$  axes as defined in the IEEE Standard, the matrices are, including the  $c_{16}$  and  $s_{16}$  entries:

$c_{11}$	$c_{12}$	$c_{13}$	0	0	$-c_{16}$	$s_{11}$	$s_{12}$	$s_{13}$	0	0	$s_{16}$
$c_{12}$	$c_{11}$	$c_{13}$	0	0	$-c_{16}$	$s_{12}$	$s_{11}$	$s_{13}$	0	0	$-s_{16}$
$c_{13}$	$c_{13}$	$c_{33}$	0	0	0	$s_{13}$	$s_{13}$	$s_{33}$	0	0	0
0	0	0	$c_{44}$	0	0	0	0	0	$s_{44}$	0	0
0	0	0	0	$c_{44}$	0	0	0	0	0	$s_{44}$	0
$c_{16}$	$-c_{16}$	0	0	0	$c_{66}$	$s_{16}$	$-s_{16}$	0	0	0	$s_{66}$

Stiffness and compliance are matrix reciprocals; the seven independent components of each are related by:

$$s_{11} = [(c_{33} / C_1) + (c_{66} / C_2)] / 2 ; s_{12} = [(c_{33} / C_1) - (c_{66} / C_2)] / 2$$

$$(s_{11} + s_{12}) = [c_{33} / C_1] ; (s_{11} - s_{12}) = [c_{66} / C_2]$$

$$s_{13} = -[c_{13} / C_1] ; s_{16} = -[c_{16} / C_1]$$

$$s_{33} = [(c_{11} + c_{12}) / C_1] ; s_{66} = [(c_{11} - c_{12}) / C_2] ; s_{44} = 1 / c_{44}$$

$$C_1 = [c_{33}(c_{11} + c_{12}) - 2 c_{13}^2] ; C_2 = [c_{66}(c_{11} - c_{12}) - 2 c_{16}^2]$$

These are inverted simply by an interchange of symbols  $c_{\lambda\mu}$  and  $s_{\lambda\mu}$ . When  $c_{16}$  is set equal to zero in the above equations, the six relations for classes 4-bar, 4, and 4/m are recovered as:

$$s_{11} = [c_{11}c_{33} - c_{13}^2] / [(c_{11} - c_{12}) C_1]$$

$$s_{12} = -[c_{12}c_{33} - c_{13}^2] / [(c_{11} - c_{12}) C_1]$$

$$s_{13} = -[c_{13} / C_1] ; s_{33} = [(c_{11} + c_{12}) / C_1]$$

$$s_{44} = 1 / c_{44} ; s_{66} = 1 / c_{66}$$

## Definition of Poisson's Ratio for Crystals

Poisson's ratio for crystals is defined in general as  $\nu_{ji} = s_{ij}' / s_{ij}'$ , where  $x_j$  is the direction of the longitudinal extension,  $x_i$  is the direction of the accompanying lateral contraction, and the  $s_{ij}'$  and  $s_{ij}'$  are the appropriate elastic compliances referred to this right-handed axial set. It suffices to take  $x_1$  as the direction of the longitudinal extension; then two Poisson's ratios are defined by the orientations of the lateral axes  $x_2$  and  $x_3$ :  $\nu_{21} = s_{12}' / s_{11}'$  and  $\nu_{31} = s_{13}' / s_{11}'$ . Application of the definition requires specification of the orientation of the  $x_k$  coordinate set with respect to the crystallographic directions, and transformation of the compliances accordingly.

## Relations for Rotated Tetragonal Compliances - General

The unprimed compliances are referred to a set of right-handed orthogonal axes related to the crystallographic axes in the manner defined by the IEEE standard. Direction cosines  $a_{mn}$  relate the transformation from these axes to the set specifying the directions of the longitudinal extension ( $x_1$ ), and the lateral contractions ( $x_2$  and  $x_3$ ). General expressions for the transformed compliances that enter the formulas for  $\nu_{21}$  and  $\nu_{31}$ , including the  $s_{16}$  terms, are:

$$s_{11}' = s_{11} [a_{11}^4 + a_{12}^4] + s_{33} [a_{13}^4] + (s_{44} + 2 s_{13}) [a_{13}^2] [a_{11}^2 + a_{12}^2] + (s_{66} + 2 s_{12}) [a_{11}^2 a_{12}^2] + 2 s_{16} [a_{11} a_{12}] [a_{11}^2 - a_{12}^2]$$

$$s_{12}' = s_{11} [a_{11}^2 a_{21}^2 + a_{12}^2 a_{22}^2] + s_{33} [a_{13}^2 a_{23}^2] + s_{44} [a_{13} a_{23}] [a_{12} a_{22} + a_{11} a_{21}] + s_{66} [a_{11} a_{12} a_{21} a_{22}] + s_{12} [a_{11}^2 a_{22}^2 + a_{12}^2 a_{21}^2] + s_{13} [a_{23}^2 (a_{11}^2 + a_{12}^2) + a_{13}^2 (a_{21}^2 + a_{22}^2)] + s_{16} [a_{21} a_{22} (a_{11}^2 - a_{12}^2) + a_{11} a_{12} (a_{21}^2 - a_{22}^2)]$$

$$s_{13}' = s_{11} [a_{11}^2 a_{31}^2 + a_{12}^2 a_{32}^2] + s_{33} [a_{13}^2 a_{33}^2] + s_{44} [a_{13} a_{33}] [a_{12} a_{32} + a_{11} a_{31}] + s_{66} [a_{11} a_{12} a_{31} a_{32}] + s_{12} [a_{11}^2 a_{32}^2 + a_{12}^2 a_{31}^2] + s_{13} [a_{33}^2 (a_{11}^2 + a_{12}^2) + a_{13}^2 (a_{31}^2 + a_{32}^2)] + s_{16} [a_{31} a_{32} (a_{11}^2 - a_{12}^2) + a_{11} a_{12} (a_{31}^2 - a_{32}^2)]$$

## Single-Axis Rotations

The general rotation relations given above for  $s_{11}'$ ,  $s_{12}'$ , and  $s_{13}'$  simplify considerably for single-axis rotations. Longitudinal extension is along the  $x_1$  axis; abbreviations  $c(\varphi)$  and  $s(\varphi)$  stand for  $\cos(\varphi)$  and  $\sin(\varphi)$ , etc.:

(A) Rotation about  $x_1$ :  $s_{11}' = s_{11}$

$$s_{12}' = s_{12} [c^2(\theta)] + s_{13} [s^2(\theta)] = s_{12} + (s_{13} - s_{12})[s^2(\theta)]$$

$$s_{13}' = s_{13} [c^2(\theta)] + s_{12} [s^2(\theta)] = s_{13} + (s_{12} - s_{13})[s^2(\theta)]$$

$$v_{21} = \{s_{12} + (s_{13} - s_{12})[s^2(\theta)]\} / s_{11} ; v_{31} = \{s_{13} + (s_{12} - s_{13})[s^2(\theta)]\} / s_{11}$$

These expressions are independent of  $s_{16}$ , and have two-fold symmetry.  
When  $\theta = \pi/4$ ,  $v_{21} = v_{31} = (s_{12} + s_{13}) / 2 s_{11}$

(B) Rotation about  $x_2$ :

$$s_{11}' = s_{11} [c^4(\psi)] + s_{33} [s^4(\psi)] + (s_{44} + 2 s_{13})[c^2(\psi)s^2(\psi)]$$

$$s_{12}' = s_{12} [c^2(\psi)] + s_{13} [s^2(\psi)] = s_{12} + (s_{13} - s_{12})[s^2(\psi)]$$

$$s_{13}' = s_{13} + s_2 [c^2(\psi) s^2(\psi)] ; s_2 = (s_{11} + s_{33} - (s_{44} + 2 s_{13}))$$

$$v_{21} = s_{12}' / s_{11}' ; v_{31} = s_{13}' / s_{11}'$$

These expressions are independent of  $s_{16}$ , and have two-fold symmetry.  
When  $\psi = \pi/4$ ,  $v_{21} = 2 (s_{12} + s_{13}) / (s_0 + s_{44})$

$$v_{31} = (s_0 - s_{44}) / (s_0 + s_{44}) ; s_0 = (s_{11} + s_{33} + 2 s_{13})$$

When  $\psi = \pi/2$ ,  $v_{21} = v_{31} = s_{13} / s_{33}$ ; Poisson's ratio is isotropic when the longitudinal extension is along the four-fold symmetry axis.

(C) Rotation about  $x_3$ :  $s_{11}' = [s_{11} + F(\phi)] ; s_{12}' = [s_{12} - F(\phi)]$

$$F(\phi) = [c(\phi)s(\phi)]\{s_1[c(\phi)s(\phi)] + 2 s_{16}[c^2(\phi) - s^2(\phi)]\}$$

$$s_1 = (s_{66} + 2 s_{12} - 2 s_{11}) ; s_{13}' = s_{13}$$

$$v_{21} = [s_{12} - F(\phi)] / [s_{11} + F(\phi)] ; v_{31} = s_{13} / [s_{11} + F(\phi)]$$

When  $\phi = \pi/4$ ,  $s_{16}$  does not appear:

$$v_{21} = [4 s_{12} - s_1] / [4 s_{11} + s_1] ; v_{31} = 4 s_{13} / [4 s_{11} + s_1]$$



### Transformation Matrix for General Rotations

In order to derive the Poisson's ratio for the most general case, we consider the transformation matrix for a combination of three coordinate rotations: a first rotation about  $x_3$  by angle  $\varphi$ , a second rotation about the new  $x_1$  by angle  $\theta$ , and a third rotation about the resulting  $x_2$  by angle  $\psi$ . When these angles are set to zero, the  $x_1, x_2, x_3$  axes coincide respectively with the reference crystallographic directions. For nonzero angles, the direction cosines  $a_{mn}$  are as follows:

$$\begin{bmatrix} [c(\varphi)c(\psi) - s(\varphi)s(\theta)s(\psi)] & [s(\varphi)c(\psi) + c(\varphi)s(\theta)s(\psi)] & [-c(\theta)s(\psi)] \\ [-s(\varphi)c(\theta)] & [c(\varphi)c(\theta)] & [s(\theta)] \\ [c(\varphi)s(\psi) + s(\varphi)s(\theta)c(\psi)] & [s(\varphi)s(\psi) - c(\varphi)s(\theta)c(\psi)] & [c(\theta)c(\psi)] \end{bmatrix}$$

Substitution of these  $a_{mn}$  into the expressions for  $s_{11}'$ ,  $s_{12}'$ , and  $s_{13}'$ , and thence into the formulas  $v_{21} = s_{12}' / s_{11}'$  and  $v_{31} = s_{13}' / s_{11}'$  formally solves the problem for specified values of  $\varphi$ ,  $\theta$ , and  $\psi$ .

### Poisson's Ratios for Specific Orientations

1) Longitudinal extension along an axis normal to the four-fold symmetry axis:  $\psi = 0$ ;  $\varphi$  and  $\theta$  arbitrary. Direction cosines are:

$$\begin{bmatrix} [c(\varphi)] & [s(\varphi)] & [0] \\ [-s(\varphi)c(\theta)] & [c(\varphi)c(\theta)] & [s(\theta)] \\ [s(\varphi)s(\theta)] & [-c(\varphi)s(\theta)] & [c(\theta)] \end{bmatrix}$$

Rotated compliances are:

$$s_{11}' = s_{11} + F(\varphi)$$

$$s_{12}' = s_{12} + (s_{13} - s_{12})[s^2(\theta)] - F(\varphi)[c^2(\theta)]$$

$$s_{13}' = s_{13} + (s_{12} - s_{13})[s^2(\theta)] - F(\varphi)[s^2(\theta)]$$

$$v_{21} = [s_{12} + (s_{13} - s_{12})[s^2(\theta)] - F(\varphi)[c^2(\theta)]] / [s_{11} + F(\varphi)]$$

$$v_{31} = [s_{13} + (s_{12} - s_{13})[s^2(\theta)] - F(\varphi)[s^2(\theta)]] / [s_{11} + F(\varphi)]$$

When  $\varphi = 0$  or  $\pi/2$ ,  $F(\varphi) = 0$ ; case (A). When  $\varphi = \pi/4$ ,  $F(\varphi) = s_1/4$ , and

$$v_{21} = [4 s_{12} + 4 (s_{13} - s_{12})[s^2(\theta)] - s_1 [c^2(\theta)]] / [4 s_{11} + s_1]$$

$$v_{31} = [4 s_{13} + 4 (s_{12} - s_{13})[s^2(\theta)] - s_1 [s^2(\theta)]] / [4 s_{11} + s_1]$$

2) Longitudinal extension along an axis not normal to the four-fold symmetry axis, but with  $x_2$  normal to the four-fold symmetry axis:  $\theta = 0$ ;  $\varphi$  and  $\psi$  arbitrary. Direction cosines are:

$[c(\varphi)c(\psi)]$	$[s(\varphi)c(\psi)]$	$[-s(\psi)]$
$[-s(\varphi)]$	$[c(\varphi)]$	$[0]$
$[c(\varphi)s(\psi)]$	$[s(\varphi)s(\psi)]$	$[c(\psi)]$

Rotated compliances are:

$$s_{11}' = [s_{11} + F(\varphi)][c^4(\psi)] + [s^2(\psi)]\{s_{33}[s^2(\psi)] + (s_{44} + 2 s_{13})[c^2(\psi)]\}$$

$$s_{12}' = s_{12}[c^2(\psi)] + s_{13}[s^2(\psi)] - F(\varphi)[c^2(\psi)]$$

$$s_{13}' = s_{13} + (s_2 + F(\varphi))[c^2(\psi)s^2(\psi)]$$

$$v_{21} = s_{12}' / s_{11}'; v_{31} = s_{13}' / s_{11}'$$

When  $\psi = \pi/4$ ,  $s_{11}' = [s_0 + s_{44} + F(\varphi)] / 4$ :

$$s_{12}' = [s_{12} + s_{13} - F(\varphi)] / 2; s_{13}' = [4 s_{13} + s_2 + F(\varphi)] / 4$$

$$v_{21} = 2 [s_{12} + s_{13} - F(\varphi)] / [s_0 + s_{44} + F(\varphi)]$$

$$v_{31} = [4 s_{13} + s_2 + F(\varphi)] / [s_0 + s_{44} + F(\varphi)]$$

When  $\psi = \pi/2$ ,  $s_{11}' = s_{33}$ ;  $s_{12}' = s_{13}$ ;  $s_{13}' = s_{13}$ :

$$v_{21} = v_{31} = s_{13} / s_{33}$$

### Conclusions

Poisson's ratio, with respect to rotated coordinate axes for tetragonal materials, has been obtained. Four cases are of particular interest:

- For longitudinal extension along  $x_1$ , and  $x_3$  along the four-fold symmetry axis:  $v_{21} = s_{12} / s_{11}$  ;  $v_{31} = s_{13} / s_{11}$

- For longitudinal extension along an axis bisecting the original  $x_1$  and  $x_3$  axes;  $x_2$  normal to the four-fold symmetry axis:

$$v_{21} = 2(s_{12} + s_{13}) / (s_0 + s_{44})$$

$$v_{31} = (s_0 - s_{44}) / (s_0 + s_{44})$$

- For longitudinal extension along the four-fold symmetry axis, the result is independent of the azimuthal angle  $\phi$ :

$$v_{21} = v_{31} = s_{13} / s_{33}$$

- For longitudinal extension along an axis bisecting the original  $x_1$  and  $x_2$  axes, and  $x_3$  along the four-fold symmetry axis:

$$v_{21} = [4 s_{12} - s_1] / [4 s_{11} + s_1]$$

$$v_{31} = 4 s_{13} / [4 s_{11} + s_1]$$

### Bibliography

[1] W G Cady, Piezoelectricity, McGraw-Hill, New York, 1946; Dover, New York, 1964.

[2] J F Nye, Physical Properties of Crystals, Clarendon Press, Oxford, 1957; Oxford University Press, 1985.

[3] R F S Hearmon, An Introduction to Applied Anisotropic Elasticity, Oxford University Press, 1961.

[4] M J P Musgrave, Crystal Acoustics, Holden-Day, San Francisco, 1970.

[5] "IEEE Standard on Piezoelectricity," ANSI/IEEE Standard 176-1987, The Institute of Electrical and Electronics Engineers, New York, 10017.

ARMY RESEARCH LABORATORY  
ELECTRONICS AND POWER SOURCES DIRECTORATE  
CONTRACT OR IN-HOUSE TECHNICAL REPORTS  
MANDATORY DISTRIBUTION LIST

February 1995  
Page 1 of 2

Defense Technical Information Center\*  
ATTN: DTIC-OCC  
Cameron Station (Bldg 5)  
Alexandria, VA 22304-6145  
(\*Note: Two copies will be sent from  
STINFO office, Fort Monmouth, NJ)

Commander, CECOM  
R&D Technical Library  
Fort Monmouth, NJ 07703-5703  
(1) AMSEL-IM-BM-I-L-R (Tech Library)  
(3) AMSEL-IM-BM-I-L-R (STINFO ofc)

Director  
US Army Material Systems Analysis Actv  
ATTN: DRXS-MP  
(1) Aberdeen Proving Ground, MD 21005

Director, Army Research Laboratory  
2800 Powder Mill Road  
Adelphi, MD 20783-1145  
(1) AMSRL-OP-SD-TP (Debbie Lehtinen)

Commander, AMC  
ATTN: AMCDE-SC  
5001 Eisenhower Ave.  
(1) Alexandria, VA 22333-0001

Director  
Army Research Laboratory  
ATTN: AMSRL-D (John W. Lyons)  
2800 Powder Mill Road  
(1) Adelphi, MD 20783-1145

Director  
Army Research Laboratory  
ATTN: AMSRL-DD (COL Thomas A. Dunn)  
2800 Powder Mill Road  
(1) Adelphi, MD 20783-1145

Director  
Army Research Laboratory  
2800 Powder Mill Road  
Adelphi, MD 20783-1145  
(1) AMSRL-OP-SD-TA (ARL Records Mgt)  
(1) AMSRL-OP-SD-TL (ARL Tech Library)  
(1) AMSRL-OP-SD-TP (ARL Tech Publ Br)

Directorate Executive  
Army Research Laboratory  
Electronics and Power Sources Directorate  
Fort Monmouth, NJ 07703-5601  
(1) AMSRL-EP  
(1) AMSRL-EP-T (M. Hayes)  
(1) AMSRL-OP-RM-FM  
(22) Originating Office

Advisory Group on Electron Devices  
ATTN: Documents  
2011 Crystal Drive, Suite 307  
(2) Arlington, VA 22202

ARMY RESEARCH LABORATORY  
ELECTRONICS AND POWER SOURCES DIRECTORATE  
SUPPLEMENTAL DISTRIBUTION LIST  
(ELECTIVE)

February 1995  
Page 2 of 2

(1) Deputy for Science & Technology  
Office, Asst Sec Army (R&D)  
Washington, DC 20310

Cdr, Marine Corps Liaison Office  
ATTN: AMSEL-LN-MC  
(1) Fort Monmouth, NJ 07703-5033

(1) HQDA (DAMA-ARZ-D/  
Dr. F.D. Verderame)  
Washington, DC 20310

(1) Director  
Naval Research Laboratory  
ATTN: Code 2627  
Washington, DC 20375-5000

(1) USAF Rome Laboratory  
Technical Library, FL2810  
ATTN: Documents Library  
Corridor W, STE 262, RL/SUL  
26 Electronics Parkway, Bldg 106  
Griffiss Air Force Base  
NY 13441-4514

(1) Dir, ARL Battlefield  
Environment Directorate  
ATTN: AMSRL-BE  
White Sands Missile Range  
NM 88002-5501

(1) Dir, ARL Sensors, Signatures,  
Signal & Information Processing  
Directorate (S3I)  
ATTN: AMSRL-SS  
2800 Powder Mill Road  
Adelphi, MD 20783-1145

(1) Dir, CECOM Night Vision/  
Electronic Sensors Directorate  
ATTN: AMSEL-RD-NV-D  
Fort Belvoir, VA 22060-5677

(1) Dir, CECOM Intelligence and  
Electronic Warfare Directorate  
ATTN: AMSEL-RD-IEW-D  
Vint Hill Farms Station  
Warrenton, VA 22186-5100